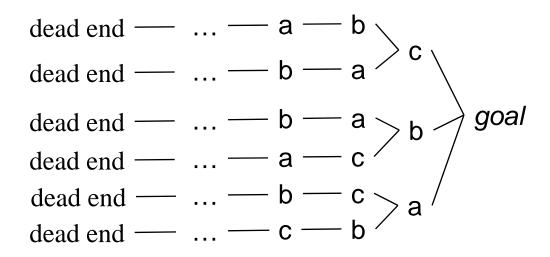
#### Lecture slides for Automated Planning: Theory and Practice

#### **Plan-Space Planning**

#### **Motivation**

- Problem with state-space search
  - ◆ In some cases we may try many different orderings of the same actions before realizing there is no solution



• Least-commitment strategy: don't commit to orderings, instantiations, etc., until necessary

#### **Outline**

- Basic idea
- Open goals
- Threats
- The PSP algorithm
- Long example
- Comments

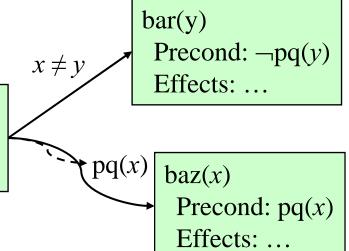
# Plan-Space Planning - Basic Idea

foo(x)

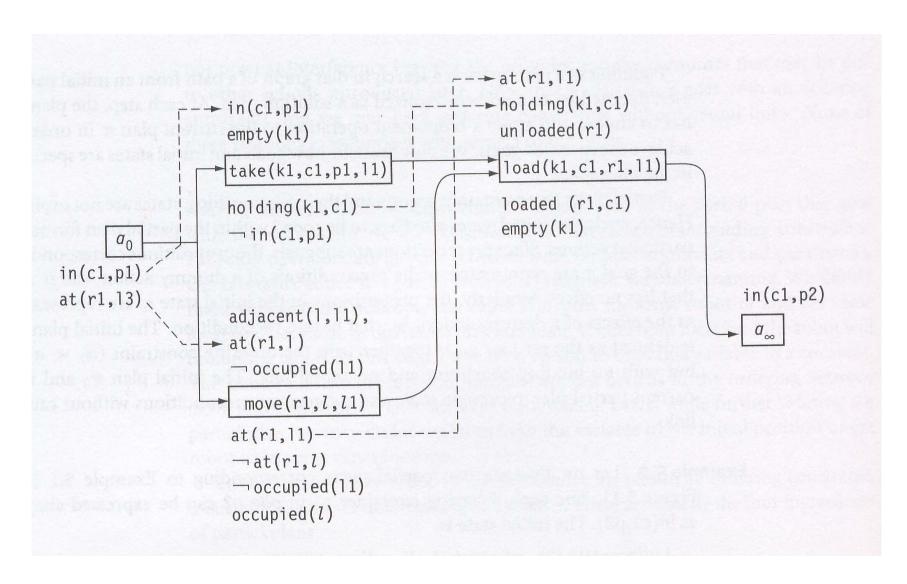
Precond: ...

Effects: pq(x)

- Backward search from the goal
- Each node of the search space is a partial plan
  - » A set of partially-instantiated actions
  - » A set of constraints
  - ◆ Make more and more refinements, until we have a solution
- Types of constraints:
  - precedence constraint: a must precede b
  - binding constraints:
    - » inequality constraints, e.g.,  $v_1 \neq v_2$  or  $v \neq c$
    - » equality constraints (e.g.,  $v_1 = v_2$  or v = c) or substitutions
  - causal link:
    - » use action a to establish the precondition p needed by action b
- How to tell we have a solution: no more *flaws* in the plan
  - Will discuss flaws and how to resolve them.

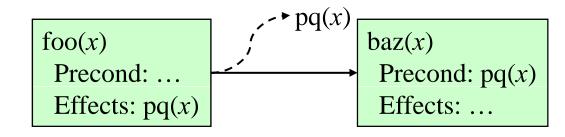


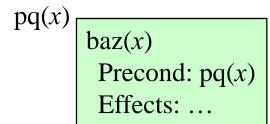
#### **An Example of Partial Plan**



# Flaws: 1. Open Goals

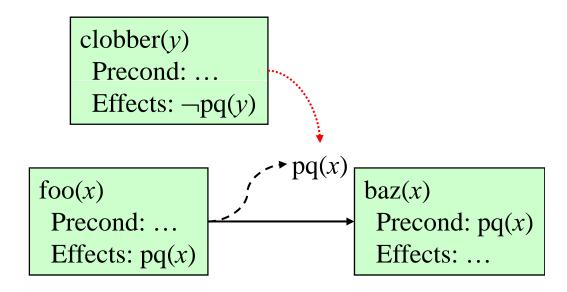
- Open goal:
  - ◆ An action a has a precondition p that we haven't decided how to establish
- Resolving the flaw:
  - ◆ Find an action b
    - (either already in the plan, or insert it)
  - that can be used to establish p
    - can precede a and produce p
  - ◆ Instantiate variables
  - ◆ Create a causal link





#### Flaws: 2. Threats

- Threat: a deleted-condition interaction
  - $\diamond$  Action a establishes a precondition (e.g., pq(x)) of action b
  - $\diamond$  Another action c is capable of deleting p
- Resolving the flaw:
  - $\diamond$  impose a constraint to prevent c from deleting p
- Three possibilities:
  - lacktriangle Make b precede c
  - ◆ Make *c* precede *a*
  - Constrain variable(s)to prevent c fromdeleting p



#### The PSP Procedure

```
\begin{split} & FSP(\pi) \\ & flaws \leftarrow \mathsf{OpenGoals}(\pi) \cup \mathsf{Threats}(\pi) \\ & \text{if } flaws = \emptyset \mathsf{ then } \mathsf{return}(\pi) \\ & \mathsf{select } \mathsf{any } \mathsf{flaw} \ \phi \in flaws \\ & resolvers \leftarrow \mathsf{Resolve}(\phi, \pi) \\ & \mathsf{if } resolvers = \emptyset \mathsf{ then } \mathsf{return}(\mathsf{failure}) \\ & \mathsf{nondeterministically } \mathsf{choose } \mathsf{a} \mathsf{ resolver} \ \rho \in resolvers \\ & \pi' \leftarrow \mathsf{Refine}(\rho, \pi) \\ & \mathsf{return}(\mathsf{PSP}(\pi')) \\ & \mathsf{end} \end{split}
```

PSP is both sound and complete

#### **Example**

- Similar (but not identical) to an example in Russell and Norvig's *Artificial Intelligence: A Modern Approach* (1st edition)
- Operators:
  - Start

Precond: none

Effects: At(Home), sells(HWS,Drill), Sells(SM,Milk),

Sells(SM,Banana)

Finish

Precond: Have(Drill), Have(Milk), Have(Banana), At(Home)

◆ Go(*I*,*m*)

Precond: At(1)

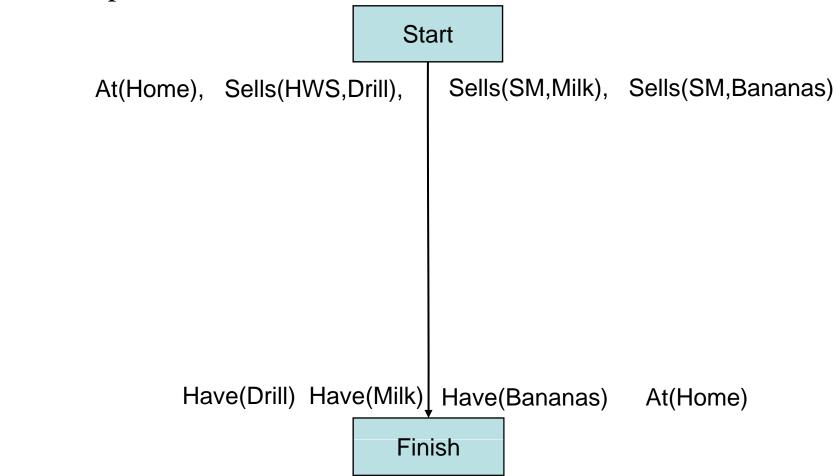
Effects: At(m),  $\neg At(l)$ 

◆ Buy(p,s)

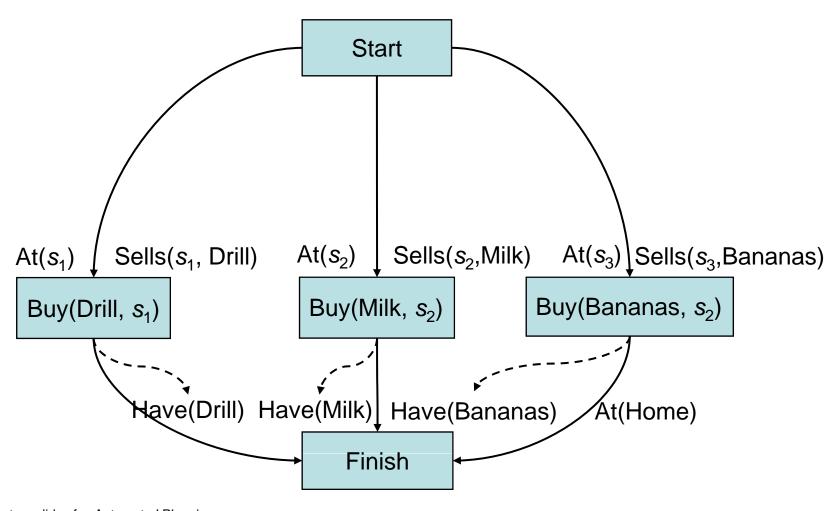
Precond: At(s), Sells(s,p)

Effects: Have(p)

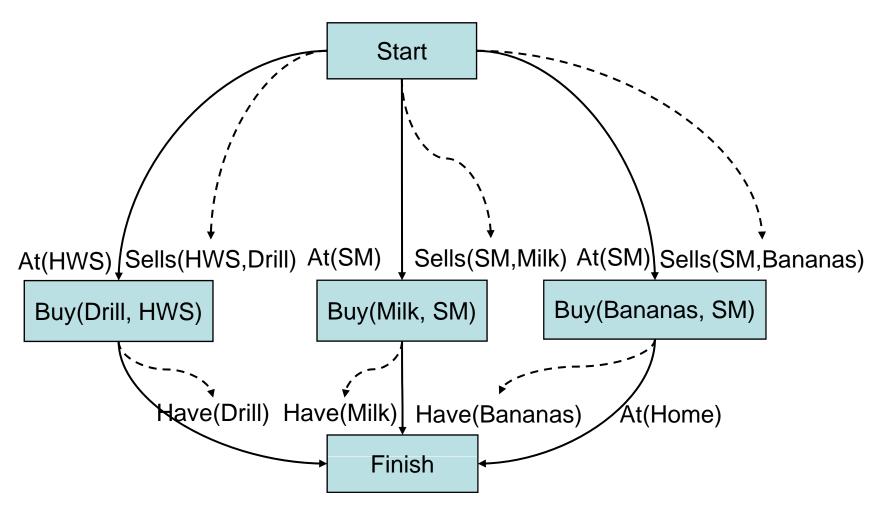
Initial plan



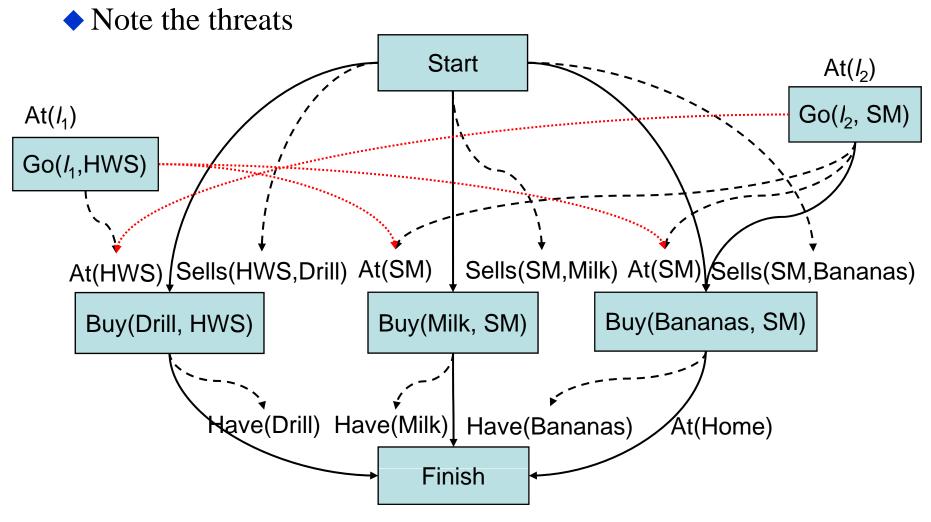
The only possible ways to establish the Have preconditions



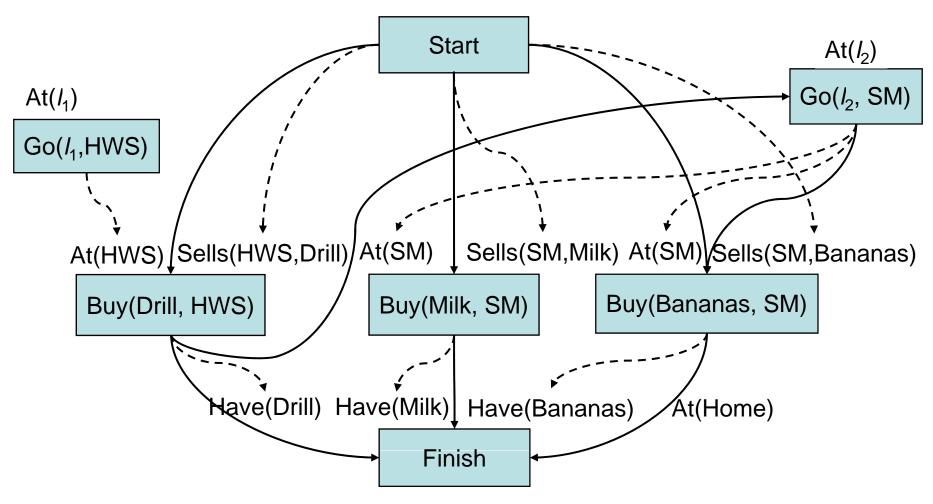
The only possible ways to establish the Sells preconditions



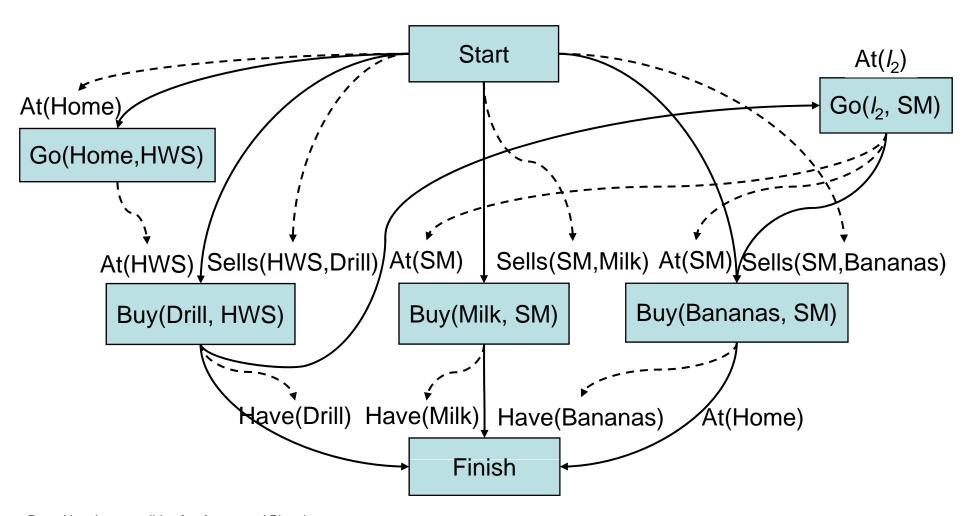
• The only ways to establish At(HWS) and At(SM)



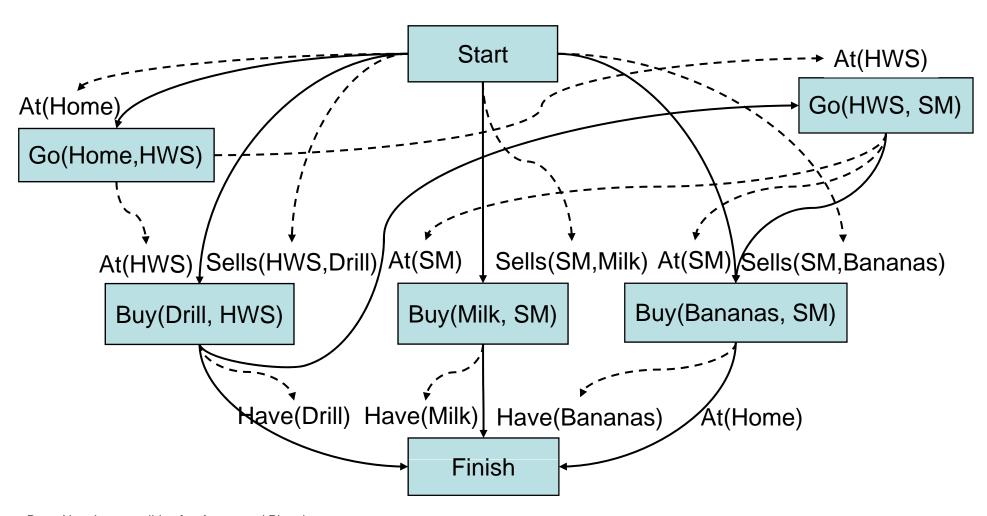
- To resolve the threat to  $At(s_1)$ , make Buy(Drill) precede Go(SM)
  - ◆ This resolves all three threats



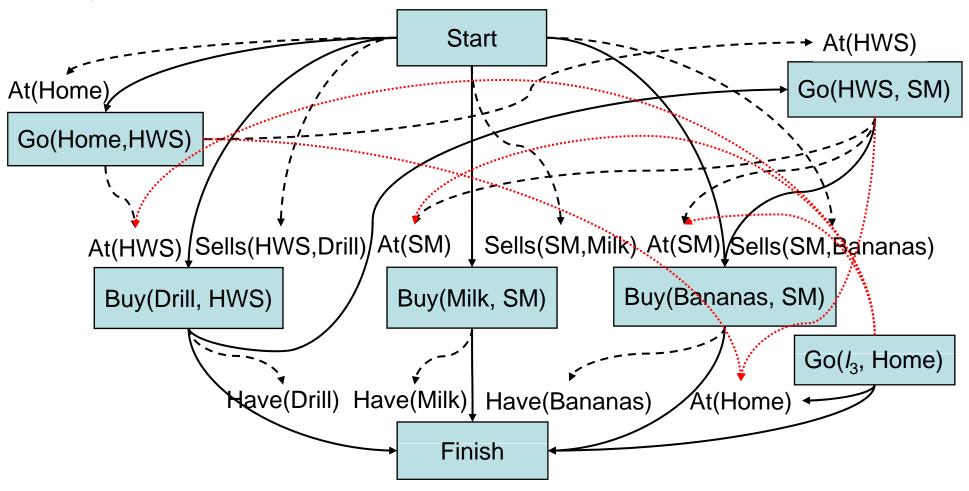
• Establish  $At(l_1)$  with  $l_1$ =Home



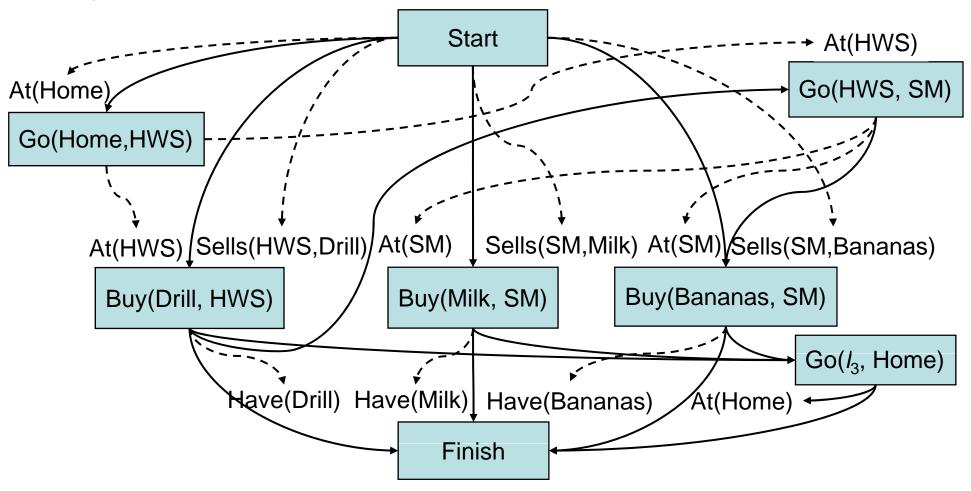
• Establish  $At(l_2)$  with  $l_2 = HWS$ 



- Establish At(Home) for Finish
  - ◆ This creates a bunch of threats

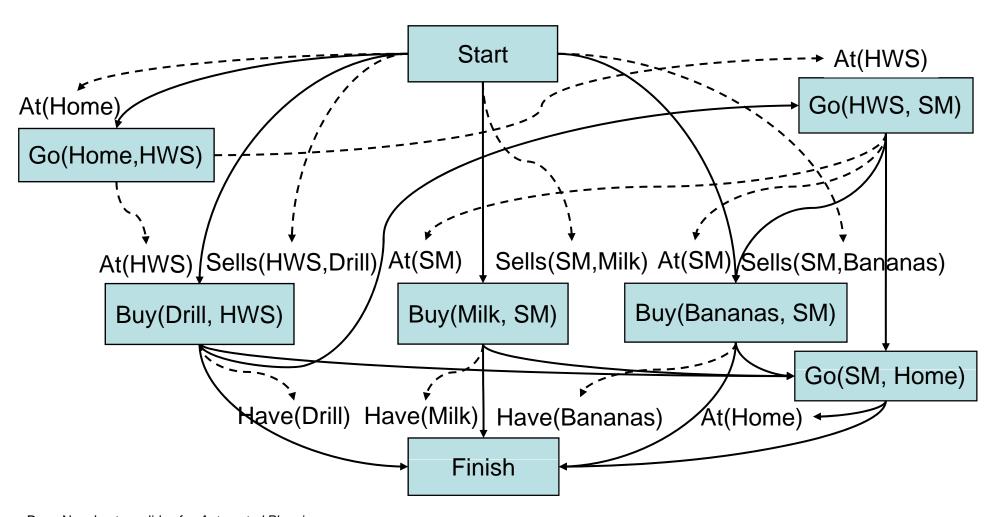


- Constrain  $Go(l_3, Home)$  to remove threats to At(SM)
  - ◆ This also removes the other threats



#### **Final Plan**

• Establish At( $l_3$ ) with  $l_3$ =SM



#### **Comments**

- PSP doesn't commit to orderings and instantiations until necessary
  - ◆ Avoids generating search trees like this one:
- Problem: how to prune infinitely long paths?
  - ◆ Loop detection is based on recognizing states we've seen before
  - ◆ In a partially ordered plan, we don't know the states
- Can we prune if we see the same *action* more than once?

$$\dots$$
 go(b,a) — go(a,b) – go(b,a) — at(a)

No. Sometimes we might need the same action several times in different states of the world (see next slide)

## **Example**

• 3-digit binary counter starts at 000, want to get to 110

$$s_0 = \{d3=0, d2=0, d1=0\}$$
  
 $g = \{d3=1, d2=1, d1=0\}$ 

Operators to increment the counter by 1:

incr0

Precond:  $d_1=0$ 

Effects:  $d_1$ –1

incr01

Precond:  $d_2 = 0$ ,  $d_1 = 1$ 

Effects:  $d_2=1$ ,  $d_1=0$ 

incr011

Precond:  $d_3=0$ ,  $d_2=1$ ,  $d_1=1$ 

Effects:  $d_3=1$ ,  $d_2=0$ ,  $d_1=0$ 

# A Weak Pruning Technique

- Can prune all paths of length > n, where  $n |\{\text{all possible states}\}|$ 
  - ◆ This doesn't help very much
- I'm not sure whether there's a good pruning technique for planspace planning